

FIGURE 2

```

procedure COMPUTEMINERROR(Aggregate  $x$ , Aggregate  $y$ , integer  $l$ )
1. if subTree[ $x$ ,  $y$ ,  $l$ ].computed = true
2.   return [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates]
3. minError := minError1 := minError2 :=  $\infty$ 
4. if  $x$  is a leaf {
5.   minError1 :=  $\sum_{s \in S} D(s, t) * (lsp(s, x, \{y\}, W_A) - lsp(s, x))$ 
6.   if  $l > 0$ 
7.     minError2 :=  $\sum_{s \in S} D(s, t) * (lsp(s, x, \{x\}, W_A) - lsp(s, x))$ 
8.   if minError1  $\leq$  minError2
9.     [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError1,  $\emptyset$ ]
10.  else
11.    [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError2,  $\{x\}$ ]
12. }
13. if  $x$  has a single child  $u$  {
14.   [minError1, aggregates1] := COMPUTEMINERROR( $u$ ,  $y$ ,  $l$ )
15.   if  $l > 0$ 
16.     [minError2, aggregates2] := COMPUTEMINERROR( $u$ ,  $x$ ,  $l - 1$ )
17.   if minError1  $\leq$  minError2
18.     [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError1, aggregates1]
19.   else
20.     [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError2, aggregates2  $\cup \{x\}$ ]
21. }
22. if  $x$  has children  $u$  and  $v$  {
23.   for  $i := 0$  to  $l$  {
24.     [minError1, aggregates1] := COMPUTEMINERROR( $u$ ,  $y$ ,  $i$ )
25.     [minError2, aggregates2] := COMPUTEMINERROR( $v$ ,  $y$ ,  $k - i$ )
26.     if minError1 + minError2 < minError
27.       minError := minError1 + minError2
28.       aggregates := aggregates1  $\cup$  aggregates2
29.   }
30.   for  $i := 0$  to  $l - 1$  {
31.     [minError1, aggregates1] := COMPUTEMINERROR( $u$ ,  $x$ ,  $i$ )
32.     [minError2, aggregates2] := COMPUTEMINERROR( $v$ ,  $x$ ,  $k - i - 1$ )
33.     if minError1 + minError2 < minError
34.       minError := minError1 + minError2
35.       aggregates := aggregates1  $\cup$  aggregates2  $\cup \{x\}$ 
36.   }
37.   [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError, aggregates]
38. }
39. subTree[ $x$ ,  $y$ ,  $l$ ].computed := true
40. return [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates]

```

FIGURE 3

```

procedure COMBINEMINERROR()
1. for  $i = 1$  to  $m$ 
2.   for  $j = 0$  to  $k$  {
3.      $T_i[j].[\text{error}, \text{aggregates}] := \text{COMPUTEMINERROR}(r(T_i), \epsilon, j)$ 
4.      $X_i[j].[\text{error}, \text{aggregates}] := [\infty, \emptyset]$ 
5.   }
6.   for  $j = 0$  to  $k$ 
7.      $X_1[j].[\text{error}, \text{aggregates}] := T_1[j].[\text{error}, \text{aggregates}]$ 
8.   for  $i = 1$  to  $m$ 
9.     for  $j = 0$  to  $k$ 
10.      for  $l = 0$  to  $j$ 
11.        if  $(X_{i-1}[l].\text{error} + T_i[j-l].\text{error} < X_i[j].\text{error})$  {
12.           $X_i[j].\text{error} = X_{i-1}[l].\text{error} + T_i[j-l].\text{error}$ 
13.           $X_i[j].\text{aggregates} = X_{i-1}[l].\text{aggregates} \cup T_i[j-l].\text{aggregates}$ 
14.        }

```

FIGURE 4

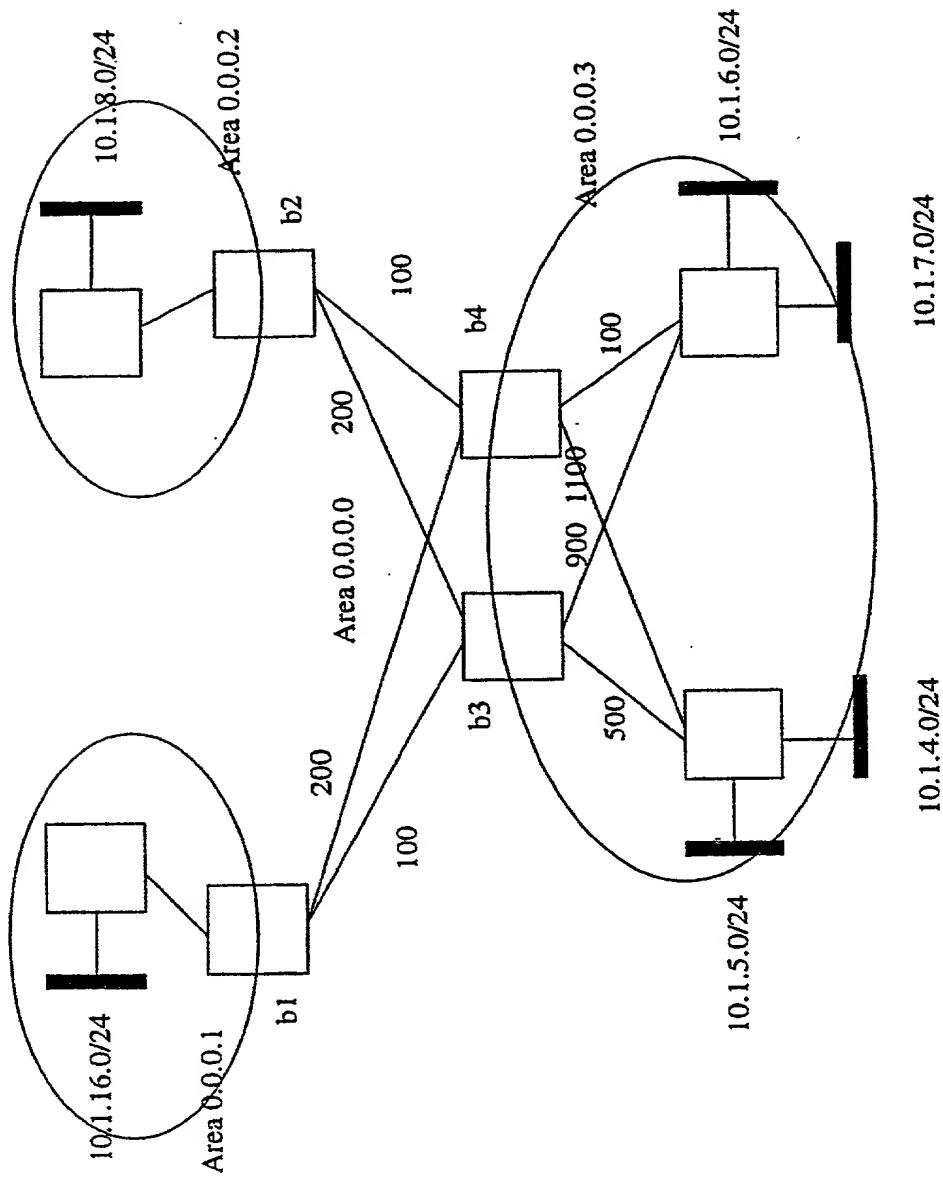


FIGURE 5

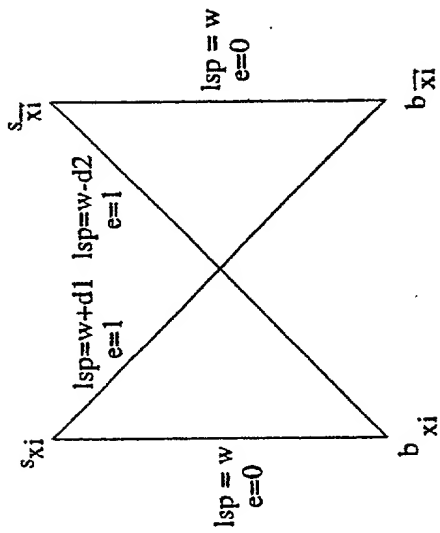
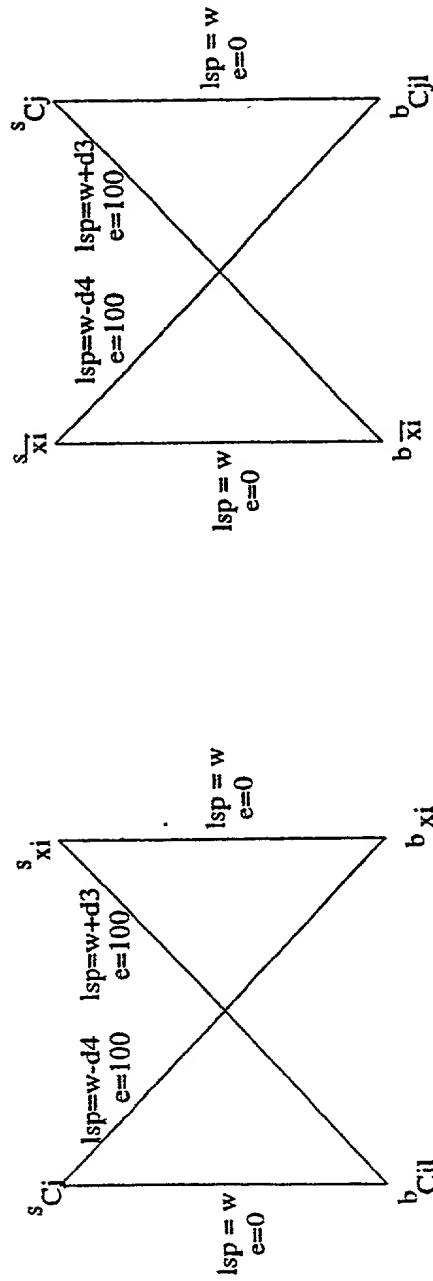


FIGURE 6



(a) $C_{ji} = x_i$

(b) $C_{ji} = \bar{x}_i$

FIGURE 7B

FIGURE 7A

```

procedure COMPUTEWEIGHTSCUMULATIVE()
1. for each  $b \in B_i$  set  $W_{min}(b) := 0$ 
2. for  $i := 1$  to  $r$  {
3.    $W := W_{min}$ 
4.   Choose a random subset  $R \subseteq B_i$  of ABRs
5.   for each  $b \in R$  set  $W(b)$  to a random weight in  $[0, L]$ 
6.   if  $\sum_{s \in S} e(s, B(s, W)) < \sum_{s \in S} e(s, B(s, W_{min}))$ 
7.      $W_{min} := W$ 
8. }
9. return  $W_{min}$ 

```

FIGURE 8

procedure ComputeWeightsMax(Q)

1. for each $b \in B_i$ set Wold(b) := 0

2. while (Pb₂B

i Wold(b) ≤ (

j B_i j*(j B_i j-1)

2) *lspmax) f3. Let

Q0 be a new set of inequalities that result when the value Wold(b) is substituted for each variable W (b) only on the LHS of each inequality in Q 4. Set Wnew(b) to the smallest possible value such that each inequality in Q0 is satisfied when Wnew(b) is substituted for variable W (b) in Q0 5. if Wnew = Wold 6. return Wnew 7. else 8. Wold := Wnew 9. g 10. return "there does not exist a weight assignment W "

FIGURE 9

procedure COMPUTEWEIGHTSTWOABR()

1. Set $V_{opt} := v(s_1)$, $E := E_{opt} := \sum_{s \in S} e(s, b_1)$
2. for $j := 1$ to n {
3. $E := E + e(s_j, b_2) - e(s_j, b_1)$
4. if $E < E_{opt}$
5. $V_{opt} := v(s_{j+1})$, $E_{opt} := E$
6. }
7. return V_{opt}

FIGURE 10